

Solution TD2

Exercise 1: (Already seen in cours, it's just a reminder)

	Base 2	Base 8	Base 10	Base 16	Smallest Base
1010	Yes	Yes	Yes	Yes	2
1020	No	Yes	Yes	Yes	3
108141	No	No	Yes	Yes	9
2A0GF00	No	No	No	No	17
01AFB	No	No	No	Yes	16
CEE	No	No	No	Yes	15
BAC	No	No	No	Yes	13

Exercise 2:

Make the following conversions:

Base 10	Base 2	Base 8	Base 16	X	Base X
555	1000101011	1053	22B	9	676
120,25	1111000.01	170,2	78,4	4	1320.1
14,5	1110.1	16.4	E,8	3	112.11111
35,05	100011.00001	43.031	23,0C	7	50.0231
45	101101	55	2D	14	33
7.34375	111.01011	7.274	7,58	6	11.20213
5.625	101.101	5.5000	5,A	3	12.12
91	1011011	133	5B	4	1123
31	11111	37	1F	5	111
684.125	1010101100.001	1254,1	2AC.2	13	408.18

190,656	10111110.1010	276,52	BE,A8	4	2332.222
162	10100010	242	A2	11	138
2655,375	101001011111.011	5137.3	A5F,6	12	1653.46
45773,164	1011001011001101.001	131315.124	B2CD,2A	7	250310.1101
17,8	10001.110011	21.63146315	11.CCCCCC	5	32.4
5	101	5	5	3	12
28	11100	34	1C	12	24
41	101001	51	29	9	45

Exercise 3:

Determine the bases in which the following numbers are expressed:

1- $(34)_x = 3 \cdot x^1 + 4 \cdot x^0 = 22 \Rightarrow 3x + 4 = 22 \Rightarrow 3x = 18$

X=6

2- The same process is applied for the rest ...

Base x	Base 10	x
34	22	6
75	117	16
1110101	117	2
24	14	5
13	7	4
70	56	8
1111	40	3
402	102	5
135	75	7
1023	75	4

Exercise 4:

1- $7 \times 3 = 21$; Convert 21 to octal: $(21)_{10} = (25)_8$

So, the octal number that is triple the value of 7 in decimal is **25**.

2- $11 \times 2 = 22$; Convert 22 to binary: $(22)_{10} = (10110)_2$

So, the binary number that is double 11 in decimal is **10110**.

3- convert 130 from decimal to ternary (base 3) $\Rightarrow$ **11211** (palindrome).

Exercise 5:

$$(\mathbf{N})_6 = \mathbf{x2y} \Rightarrow x \times 6^2 + 2 \times 6^1 + y \times 6^0 \Rightarrow 36x + 12 + y$$

$$(\mathbf{N})_5 = \mathbf{3x2} \Rightarrow 3 \times 5^2 + x \times 5^1 + 2 \times 5^0 \Rightarrow 75 + 5x + 2$$

$$36x + 12 + y = 75 + 5x + 2 \Rightarrow 36x - 5x = 77 - 12 - y \Rightarrow 31x = 65 - y$$

y takes values from 0 to 4 $\Rightarrow$

$$y = 0 \Rightarrow x?$$

$$y = 1 \Rightarrow x?$$

$$y = 2 \Rightarrow x?$$

$$\mathbf{y = 3 \Rightarrow x = 2}$$

$$y = 4 \Rightarrow x?$$

$$(\mathbf{N})_6 = \mathbf{x2y} \Rightarrow (\mathbf{223})_6 = (\mathbf{87})_{10}$$

Exercise 6:

Convert 41346460 from decimal to base 5:

$$(41346460)_{10} = (410 \ 410 \ 41320)_5 = (\mathbf{COT \ COT \ CODET})_5$$

$$\mathbf{C = 4}$$

$$\mathbf{O = 1}$$

$$\mathbf{T = 0}$$

$$\mathbf{D = 3}$$

$$\mathbf{E = 2}$$

Exercise 7: (Already seen in cours, it's just a reminder)

1. $a_i < 5$ so, $a_i \in \{0, 1, 2, 3, 4\}$; $b_i < 7$ so, $b_i \in \{0, 1, 2, 3, 4, 5, 6\}$;

2.
$$\begin{cases} A+B = (138)_9 \\ A-B = (200)_6 \end{cases}$$
 The sum of these two equations gives : $2A = (138)_9 + (200)_6$

You must convert the two operands to the same base to perform the operation.
The best choice is to convert them to a decimal base.

$$\left. \begin{aligned} (138)_9 &= 1 \times 9^2 + 3 \times 9^1 + 8 \times 9^0 = (116)_{10} \\ (200)_6 &= 2 \times 6^2 + 0 \times 6^1 + 0 \times 6^0 = (72)_{10} \end{aligned} \right\} \begin{aligned} 2A &= 116 + 72 \leftrightarrow \underline{A} = (94)_{10} \\ B &= 116 - A \leftrightarrow B = (22)_{10} \end{aligned}$$

$$\left\{ \begin{aligned} A &= (94)_{10} = (??)_5 \\ B &= (22)_{10} = (??)_7 \end{aligned} \right. \text{ By the method of successive divisions, we find: } \left\{ \begin{aligned} A &= (334)_5 \\ B &= (031)_7 \end{aligned} \right.$$

By identification: $a_3 = 3$; $a_2 = 3$; $a_1 = 4$
 $b_3 = 0$; $b_2 = 3$; $b_1 = 1$

3.
$$\begin{cases} A = (94)_{10} = (1011110)_2 \\ B = (22)_{10} = (10110)_2 \end{cases}$$

$$\begin{array}{r} A \quad 1 \quad 10 \quad 11 \quad 11 \quad 11 \quad 1 \quad 0 \\ + \\ B \quad 0 \quad 0 \quad 1 \quad 0 \quad 1 \quad 1 \quad 0 \\ = \quad 1 \quad 1 \quad 1 \quad 0 \quad 1 \quad 0 \quad 0 \end{array}$$

$$\begin{array}{r} A \quad 1 \quad 0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 0 \\ - \\ B \quad 0 \quad 0 \quad 1 \quad 0 \quad 1 \quad 1 \quad 0 \\ = \quad 1 \quad 0 \quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \end{array}$$

B					
1	0	1	1	0	0
			1	0	0
			1	0	0
			1	0	0
			1	0	0

A						1	0	1	1	1	1	0
*												
B/100									1	0	1	1
=												
						11	0	1	1	1	1	0
+						01	0	1	1	1	1	0
+						110	0	0	0	0	0	0
+						1	1	1	1	0	0	0
=						1	0	0	0	1	0	0

A						B					
1	0	1	1	1	1	1	0	1	1	0	
						1	0	0	0	1	
						1	1	0	0	0	
						-	1	0	1	1	0
							0	0	0	1	0
											

Exercise 8:

$$(1011.1101)_2 + (11.1)_2 = (1111.0101)_2$$

$$(1010.0101)_2 - (110.1001)_2 = (11.11)_2$$

$$(110)_2 * (1.01)_2 = (111.1)_2$$

$$(91B)_{16} + (6F2)_{16} = (100D)_{16} = (10015)_8$$

Exercise 9:

Decimal	Binary	SVA	C1	C2	Excess
1	00000001	00000001	00000001	00000001	10000000
-1	00000001	10000001	11111110	11111111	11111110
-99	01100011	11100011	10011100	10011101	00011100
-24	00011000	10011000	11100111	11101000	01100111
127	01111111	01111111	01111111	01111111	01111111
-128	0000000010000000	1000000010000000	1111111101111111	1111111110000000	1011101001110001

Exercice 10:

Example:

13.25

Method

- Integer part : $13 \Rightarrow 1101$
- Decimal part : $0,25 \Rightarrow 0,01$
- $(13.25)_{10} = (1101,01)_2$
- Normalization : $1101,01 \times 2^0 \Leftrightarrow 0.110101 \times 2^4$
- Pseudo-normalization IEEE 754 : $\Leftrightarrow 1.10101 \times 2^3$ (in format of 1,xxxx where xxx = pseudo mantissa)

Decomposition of Number into its various elements:

- Sign bit: 0 (Number positif)
- Exponent on 8 bits biased by 127 $\Rightarrow 3 + 127 = 130 \Rightarrow 1000\ 0010$
- Pseudo mantissa on 23 bits: 1010 1000 0000 0000 0000 0000

Sign	Biased exponent	Pseudo mantissa
0	1000 0010	1010 1000 0000 0000 0000 000

Decimal	Representation in IEEE 754-32 format		
	Sign	Exponent	Mantissa
$N1 = (-6.53125)_{10}$	1	10000001	10001000000000000000000
$N2 = (-32.625)_{10}$	1	10000100	10100000000000000000000
$N3 = (-11.8561)_{10}$	1	10000011	11100011000001111101000

Exercise 11:

	Sign	exponent	Mantissa
1	1	1000 0010	1010 1000 0000 0000 0000 000
	-	$130 = 127 + 3 \Rightarrow \text{puissance } 3$	10101
	-	2^3	$\times 1.10101$

The result is $-1.10101 \times 2^3 = (-1101.01)_2 = (-13.25)_{10}$

	Sign	exponent	Mantissa
2	1	1000 0100	1001 0100 0000 0000 0000 000
	-	$132 = 127 + 5 \Rightarrow \text{puissance } 5$	1001 01
	-	2^5	$\times 1.1001 01$

Result is $-1.1001 01 \times 2^5 = (-110010.1)_2 = (-50.5)_{10}$

	Sign	exponent	Mantissa
3	0	10001010	11111000000000000000000000000000
	+	$138 = 127 + 11 \Rightarrow \text{puissance } 11$	1111 1
	+	2^{11}	$\times 1.1111 1$

The result is $+1.1111 1 \times 2^{11} = (+1111 1100 0000)_2 = (+16128)_{10}$